## Math 227S: Statistics with Support

## Course Content and Objectives

| COURSE CONTENT AND SCOPE <br> - Lecture: Outline the topics included in the lecture portion of the course (Outline reflects course description, all topics covered in class). | Hours Per Topic | COURSE OBJECTIVES - Lecture: Upon successful completion of this course, the student will be able to...(Use action verbs - see Bloom's Taxonomy for 'action verbs requiring cognitive outcomes.') |
| :---: | :---: | :---: |
| Qualitative and quantitative description of data; and design of experiments. | 6 | Describe, explore, and compare data; explain the characteristics of a properly designed experiment; define a population parameter; define a sample statistic; know the difference between discrete and continuous data; understand the nominal, ordinal, interval and ratio levels of measurement; critically examine a sample to determine if it is a simple random sample; discuss sampling strategies including random, simple random, systematic, convenience, stratified and cluster sampling; explain the characteristics of an observational study, an experiment, a cross-sectional study, a retrospective study, and a prospective study; and understand the effects of confounding, blinding, placebos, blocks, replication and sample size in the design of experiments. |
| Frequency distributions; visualizing data; measures of center; measures of variation; measures of relative standing; and exploratory data analysis (EDA). | ${ }^{6}$ | Summarize data graphically and numerically. Given a set of data: Construct a histogram, frequency polygon, cumulative frequency polygon, ogive, dot plot, stem-and-leaf plot, and box plot; calculate the mean, mode, median, and weighted means; calculate the standard deviation, range, variance, and range rule of thumb; apply Chebyshev's Theorem; calculate the mean absolute deviation; calculate the mean, standard deviation and median of grouped data; calculate zscores; determine unusual and ordinary values; calculate quartiles and percentiles; determine outliers; investigate the data set to understand and describe its important characteristics such as its center, variation, distribution, outliers, and any changing characteristics of the data over time. |
| Probability: Addition rule, multiplication rule, complements; conditional probability; Bayes' Theorem; and counting. | 4 | State the rare event rule for inferential statistics; define event, simple event, and sample space; understand the relative frequency approximation of probability, the classical approach to probability, and subjective probabilities; state the law of large numbers; determine the complement of an event; calculate odds; define and calculate probabilities for compound events; state and use the addition rule; define disjoint or mutually exclusive events; use complementary events to calculate probabilities; use tree diagrams to describe a sample space; define conditional probabilities; apply Bayes' Theorem; define independent and dependent events; use the multiplication rule for dependent and independent events; calculate conditional probabilities; test for independence of events; define simulations; and apply the fundamental counting rule, the factorial rule, the permutations rule with different items, the permutations rule when some items are the same, and the combinations rule. |
| Probability distributions: Random variables; binomial distribution; mean, variance, and | 6 | Define random variable, both discrete and continuous; define probability distribution; calculate the mean, variance, and standard deviation for a probability |

standard deviation for the binomial distribution; and Poisson distribution.
distribution; define and calculate the expected value of a discrete random variable; define the characteristics of a binomial probability distribution; use the binomial probability formula, calculate the mean, variance, and standard deviation for the binomial distribution; define the Poisson distribution, use the probability formula for the Poisson distribution; and approximate the binomial distribution with the Poisson distribution when the number of trials is large and the probability of a success is small.

| Normal probability distributions: Standard 6 | Define and graph a normal distribution, a uniform |
| :--- | :--- | :--- | normal distribution, applications, sampling distributions, estimators; the Central Limit Theorem; normal distribution as an approximation to the binomial distribution; and determining normality.


$\left.$|  |  | the means; determine the standard error of the mean; <br> apply the correction for a finite population to the <br> standard deviation of the sampling means; know the <br> conditions in which a normal distribution in an <br> approximation to the binomial distribution; know how to <br> make continuity corrections when the normal distribution <br> is used to approximate the binomial distribution; <br> construct a normal quantile plot; and determine whether <br> data have a normal distribution with the aid of a normal <br> quantile plot. |
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| Estimate and sample sizes: Estimating a <br> population proportion, a population mean, or a <br> population variance; and Student t and chi- <br> squared distributions. | State the assumptions used in estimating a population <br> proportion, mean, or variance; give the best point <br> estimate for a population proportion, mean, or variance; <br> define and construct confidence intervals; define the <br> confidence level, degree of confidence, or confidence <br> coefficient; interpret a confidence interval; define and <br> compute the margin of error; determine the sample size <br> needed to estimate a population proportion, mean, or <br> variance; and use the Student t-distribution in estimates. |  |
| Hypothesis testing: Testing claims about <br> proportions, means, standard deviations, or <br> variances. | Define hypothesis, null hypothesis, and alternative <br> hypothesis; calculate a test statistic; define and <br> determine the critical region, significance level, critical <br> value, and P value; define Type I and II errors; and <br> restate the conclusion of the hypothesis test in layman's <br> terms. Perform t-test and chi-square test for one |  |
| population. Apply these techniques to application |  |  |
| problems using data from disciplines including business, |  |  |
| social sciences, psychology, political science, life |  |  |
| sciences, health science, information technology, and |  |  |
| education. Perform statistical analysis using technology |  |  |
| such as Minitab, graphing calculator, SPSS, or Microsoft |  |  |
| Excel. |  |  |\(\left|\begin{array}{l}Perform hypothesis tests on two population parameters; <br>

determine the confidence interval estimate of the <br>
difference of two population parameters; state the <br>
assumptions used in making inferences about two <br>
population parameters; draw inferences from matched <br>
pairs of data; and compare variation in two samples <br>

using the F distribution.\end{array}\right|\)| Define correlation between two variables; draw a |
| :--- |
| scatterplot of scatter diagram of paired data; compute |
| the linear correlation coefficient; perform a hypothesis |
| test for correlation; find the regression equation for |
| paired data; use the regression equation for predictions; |
| calculate the residual; calculate the unexplained, | \right\rvert\,


|  |  | explained, and total deviation; calculate the coefficient of <br> determination; compute the standard error of estimate <br> and the prediction interval in paired data; compute the <br> multiple regression equation between a dependent <br> variable and two or more independent variables; and <br> develop a mathematical model to fit or describe a given <br> data set. |
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| Multinomial experiments: Goodness of fit. <br> Contingency tables: Independence and <br> homogeneity. | 6 | Define multinomial experiment; perform a goodness-of- <br> fit test; define contingency table; define test of <br> independence; perform a test of independence on a <br> contingency table; calculate expected frequency for a <br> contingency table; and perform a test of homogeneity. |
| Analysis of Variance (ANOVA): One-way <br> ANOVA, two-way ANOVA. | 6 | Define analysis of variance (ANOVA); use the F <br> Distribution in ANOVA; perform a one-way ANOVA (or <br> single factor ANOVA) on three or more populations with |
| equal or unequal sample sizes; define treatment or |  |  |
| factor; state the assumptions made in a one-way |  |  |
| ANOVA; define interaction between two factors; perform |  |  |
| the procedure for two-way ANOVA; and state the |  |  |
| assumptions made in two-way ANOVA. |  |  |$|$

*Total lecture and laboratory hours (which include the final examination) must equal totals on page 1.
**In general "activity" courses or portions of courses are classified "laboratory."

## 1. LAB:

| COURSE CONTENT AND SCOPE - Lab: Outline the topics included in the lecture portion of the course (Outline reflects course description, all topics covered in class). | $\begin{array}{\|l} \hline \text { Hours } \\ \text { Per } \\ \text { Topic } \end{array}$ | COURSE OBJECTIVES - Lab: Upon successful completion of this course, the student will be able to...(Use action verbs see Bloom's Taxonomy for 'action verbs requiring cognitive outcomes. ') |
| :---: | :---: | :---: |
| Fractions, decimals, and percents. Significant digits, place value, and scientific notation. | 3 | Perform conversions among fractions, decimals, and percent. Define significant digits. Round decimal numbers to the given place value. Perform conversions between scientific notation and decimal notation. |
| Exponents, square roots, and order of operations. | 3 | Simplify expressions with square roots and exponents. Evaluate expressions using the order of operations. |
| Summation. | 0.5 | Evaluate expressions using summation notation. Find the sum of a list of values. |
| Statistical technology, such as TI graphing calculators, Excel, Minitab, or other statistical software packages. | 2 | Compute descriptive statistics, including mean, standard deviation, and variance, draw graphs, construct confidence intervals, and perform hypothesis testing. |
| Linear equations in two variables including standard form, slope-intercept form, and the pointslope form. Graphs, estimation, and predictions. | 3 | Graph linear equations in standard form and in slope-intercept form. Interpret the slope and the $y$-intercept for linear applications modeled by a linear equation. Formulate the equation of a line given the slope and a point, and given two points on the line. Estimate the $y$-values based on the given $x$ values. Interpret the results. |
| Linear equations and linear inequalities in one variable. Solving equations and Inequalities. | 3 | Translate key words such as "at most" and "at least" into a mathematical inequality. Solve linear equations and inequalities containing integers, fractions, and decimals. Solve equations and inequalities for a specified variable. |
| Set theory and Venn diagrams. | 0.5 | Construct Venn diagrams to represent operations for sets, such as union, intersection, and complement. |
| Tree diagrams, sample spaces, and probability. | 1 | Construct tree diagrams to find sample spaces for a sequence of experiments; compute basic probabilities of events. |
| Counting theory. | 1.5 | Solve counting problems using the multiplication principle, permutations, and combinations. |
| Contingency tables. | 0.5 | Interpret contingency tables. Perform computations using contingency tables and interpret the results. |
| Total Lab Hours In Section I Class Hours: | $\begin{aligned} & 18 \\ & 18 \\ & \hline \end{aligned}$ |  |

